

Machine learning: a hands-on introduction

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Supervised learning

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What is learning?





- building a statistical model for predicting an output based on one or more inputs
- statistical learning model is **trained** rather than explicitly programmed

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What is learning?





- building a statistical model for predicting an output based on one or more inputs
- statistical learning model is trained rather than explicitly programmed
- ML models do not learn by trying to understand what goes on, rather by trial and error through a vast number of examples (not like a university student but like a little child)

What is learning?





- 1. <u>Input data</u> (e.g. genome variants, metabolites)
- 2. <u>Output examples</u> (e.g. disease status, biological characteristics)
- 3. <u>Performance measure</u>: how well is the algorithm working \rightarrow adjustment steps \rightarrow learning

You can do (statistical) learning in your head

- The current price of an electric Tesla is \$100,000
- The price of an electric Tesla next year will be \$90,000

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- The price of an electric Tesla in two years will be \$81,000
- The price of an electric Tesla in three years will be \$72,900
- How much will an electric Tesla cost in five years?

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You can do (statistical) learning in your head

TRAINING DATA

- The current price of an electric Tesla is \$100,000
- The price of an electric Tesla next year will be \$90,000
- The price of an electric Tesla in two years will be \$81,000
- The price of an electric Tesla in three years will be \$72900
- How much will an electric Tesla cost in five years?

NEW, UNKNOWN DATA

 $PRICE = PRICE_0^{(1-0.10)} YEARS$

PRICE IN FIVE YEARS= \$59,049

MATHEMATICAL PREDICTION MODEL MODEL

The truth about learning

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- Yesterday: **n. of cases = 2**^(days-1)
- Today: price = price_0 * (1-0.10)^{years}

Is this what ML is learning?

The truth about learning





- (known) quadratic function
 (blue line)
- approximated with machine learning (orange line)

Why supervised?





Unsupervised learning





The steps of a supervised learning problem



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A little ML jargon



	Sepal.Length	Sepal.Width 🔷	Petal.Length ≑	Petal.Width 🚊	Species
• example (record, observation)	5.0	2.0	3.5	1.0	versicolor
	6.2	2.2	4.5	1.5	versicolor
feature (independent variable factor)	6.0	2.2	4.0	1.0	versicolo
	6.0	2.2	5.0	1.5	virginica
labal (dependent variable)	6.3	2.3	4.4	1.3	versicolo
	5.5	2.3	4.0	1.3	versicolo
	5.0	2.3	3.3	1.0	versicolo
method : the statistical method used for a problem	4.5	2.3	1.3	0.3	setosa
	5.5	2.4	3.8	1.1	versicolo
model : the modelling of the problem (e.g. which	5.5	2.4	3.7	1.0	versicolo
	4.9	2.4	3.3	1.0	versicolo
features to include and how)	6.7	2.5	5.8	1.8	virginica
	6.3	2.5	4.9	1.5	versicolor
algorithm: the technique by which the method is					

- algorithm: the technique by which the method is applied to the model and solved
- training data: data on which the ML algorithm is trained



Regression and classification

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- Regression (**predictive**) problems
 - target (continuous) variable, output
- Classification (predictive) problems
 - label, class (qualitative variable): binomial, multinomial, ordinal, nominal

"given a set of data, the learning algorithm attempts to optimize a function (the model) to find the combination of feature values that result in the target output"



- Regression (**predictive**) problems
 - target (continuous) variable, output
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Predict:

- the future (forecasting, prognosis)
- the unknown/unseen (e.g. sick/healthy, genetic predisposition etc.)
- real time (e.g. control traffic lights at rush hours)
- the past (e.g. when something happened, like conception date based on hormone levels)





- Know the past
- Predict the future
- Act consequently





- Know the past
- Predict the future
- Act consequently

Inference vs Prediction





- different statistical problems
- different objectives, different rules ... different ballparks
- inference is in general more difficult than prediction

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- Typical inferential problem
- Correlation is not causation!
 - already since Pearson! (early 1900's)
 - spurious correlations generator
 - apophenia (from Greek, "to seem")



- Typical inferential problem
- Correlation is not causation!

Reverse causation

- n. of firemen ←→size of the fire (the more the firemen, the bigger the fire?)
- smoking ← →depression (smoking causes depression?)

Missing variable

- ice cream consumption $\leftarrow \rightarrow n$. of sunburn cases
- buying lighters ← →lung cancer





- Typical inferential problem
- Correlation is not causation!

Reverse causation

- n. of firemen \leftarrow \rightarrow size of the fire (the more the firemen, the bigger the fire?)
- smoking $\leftarrow \rightarrow$ depression (smoking causes depression?)

Missing variable

- ice cream consumption $\leftarrow \rightarrow n$. of sunburn cases
- buying lighters $\leftarrow \rightarrow$ lung cancer



3.6

Q: reverse causation or missing variable?

Fig.1

S FACEBOOK DRIVING THE GREEK DEBT CRISIS?

Number

ofactive

Facebook user:



16.82

2011

750m users



- Also regression!
 - **Galton**: predict the height of children from the height of their parents
 - But also the height of parents could be predicted from that of their children!
 (??)→no possible cause-effect relationship!



[Han, Ma, Zhu 2015]



MY RESEARCH SUGGESTS THE EXISTENCE OF AN 800-METER SPHERE THAT TASTES OKAY. Physalia Courses

spurious regression: can you spot the mistakes?

The probabilistic nature of cause (it gets trickier)

- you turn the key and the car engine starts: clear cause-effect link
- you take an ibuprofen pill and your headache goes away: how do you know it wouldn't have gone anyway? → counterfactual
- smoking→lung cancer: my uncle always smoked and did not have lung cancer! my aunt never smoked and got lung cancer! →if you smoke it is more likely that you get lung cancer

 $X \rightarrow Y$: X increases/decreases the chances that Y happens



[Heart Protection Study, 2002: https://www.thelancet.com/journals/lancet/article/PIIS0140-6736(02)09327-3/fulltext]

placebo % statin % relative risk reduction

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The probabilistic nature of cause (it gets trickier)



- **experiments** (RCT, A/B testing etc.)

without experiments

- post hoc, ergo propter hoc
- strength of correlation
- consistency (different datasets, studies etc.)
- dose-response relationship
- analysis "ceteris paribus" (controlling for confounders, stratifiers etc.)
- Bayesian Networks

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What causes what? ML perspective



"observational data alone does not provide causal insight" (Pearl and Mackenzie 2018*)

ML can help with causal questions:

- studying associations between variables: starting point for causal hypotheses
- estimating causal effects: quantify the dose-response relationship
- learning causal models: tools to reason about interventions and counterfactuals
- learning causal graphs: direction of causal relationships
- etc.

The gist of it: if you can predict y using x, then there probably is a causal relationship between x and y

*Pearl, J. and Mackenzie, D., 2018. The book of why: the new science of cause and effect. Basic books

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- Regression (predictive) problems
- Classification (predictive) problems

Predictive machines!

- Classifiers
- Predictors/Regressors



source:

https://blog.bigml.com/2013/03/12/machine-learning-from-streaming-data-two-problems-two-solutions-two-concerns-and-two-lessons/



Regression

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Regression problems

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- the response variable **y** is **quantitative**
- e.g.: height, weight, yield (milk, crops), blood sugar concentration

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- **y** = **target** (dependent) variable (a.k.a. response, objective variable)
- **X** = matrix of **features** (continuous, categorical)
- predictor: y = f(x) = P(X) ← [predictive machine]

Regression problems - simple regression



happiness = (intercept) + beta*income

or

income = (intercept) + beta*happiness

Source: https://www.scribbr.com/statistics/linear-regression-in-r/



Regression problems - multiple regression

Source: https://aeqis4048.github.io/mutiple linear regression and visualization in python

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Multiple linear regression



$y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p + \epsilon$

- y: target variable
- β's: model coefficients
- X's: features (predictors, independent variables, factors)

Multiple linear regression

 $\mathbf{y} = \beta \mathbf{X} + \mathbf{e}$



- matrix (compact) notation
- vectors of observations (y), coefficients
 (β) and residuals (e)
- matrix of features (X)

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Multiple linear regression





- matrix (compact) notation
- vectors of observations (y), coefficients
 (β) and residuals (e)
- matrix of features (X)

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 $\hat{y} = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p$

with the estimated coefficients ${\bf \beta}$ and the feature values ${\bf X}$ we obtain the predicted values \hat{y}





 $\hat{y} = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p$

with the estimated coefficients ${\bf \beta}$ and the feature values ${\bf X}$ we obtain the predicted values \hat{y}

 \rightarrow how do we obtain the model coefficients β ?



 $y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p + \epsilon$

define a loss (cost) function
minimise the loss function

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- define a loss (cost) function

observations	predictions		
У	$\mathbf{\hat{y}} = \hat{\beta} \mathbf{X}$		

difference between observed and predicted values



- define a loss (cost) function

observations	predictions
У	$\mathbf{\hat{y}} = \mathbf{\hat{\beta}} \mathbf{X}$

difference between observed and predicted values

LEAST SQUARES

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- minimise the loss (cost) function

$$RSS = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$
 $RSS = \sum_{i=1}^n (y_i - \hat{eta}_i X_i)^2$

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LEAST SQUARES

 $\underset{(\beta)}{\text{minimize }} (RSS)$

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- minimise the loss (cost) function

$$J(\beta) = \frac{1}{2n} \sum_{i=1}^{n} (\beta_i X_i - y_i)^2$$

$$\underset{\beta}{\text{minimize } J(\beta)}$$

$$\underset{\beta}{\text{modified (normalized) RSS function}}$$











Multiple linear regression (e.g.

2 parameters):

 $y=eta_0+eta_1\cdot x$





Multiple linear regression (e.g.

2 parameters):

$$y=eta_0+eta_1\cdot x$$

Multiple linear regression (> 2 parameters):

 \rightarrow m-dimensional hyperspace





- Demonstration 1.1
- Exercise 1.1

 \rightarrow 1.introduction_to_ml.Rmd



Minimising the cost function



- the defined cost function is **convex** (it has a minimum!)
- we saw an <u>empirical approach</u> to finding the minimum (manually try some values for the parameters) and the <u>least squares</u> approach

how do we minimise the cost function in machine learning?

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Minimising the cost function



- can be minimised by gradient descent
- machine learning perspective: gradient descent is a general algorithm to solve models
- alternatively:
 - maximum likelihood
 - (non-)linear least squares

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Loss function: finding the minimum?

Gradient Descent:

 $\underset{\beta}{\text{minimize}} J(\beta)$

- 1. Start with initial values for β
- 2. Change β in the direction of reducing J(β)
- 3. Stop when the minimum is reached

: (initialisation)

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- : (descent)
- : (minimisation)





starting point (initialisation)

- find the steepest direction around the starting point
- take one step in this direction
- . repeat until convergence (local minimum)

Source: Andrew Ng https://medium.com/@DBCerigo/on-why-gradient-descent-is-even-needed-25160197a635





starting point (initialisation)

- . find the steepest direction around the starting point
- take one step in this direction
- . repeat until convergence (local minimum)

changing initialisation may lead to a different local minimum!

Source: Andrew Ng https://medium.com/@DBCerigo/on-why-gradient-descent-is-even-needed-25160197a635









Z made with













- α controls the size of the updating step
- large $\alpha \rightarrow$ overshooting: failure to converge

 $eta_j := eta_j - lpha rac{\partial}{\partial eta_j} J(eta)$

Gradient descent - recap



- general method to **solve machine learning models** (e.g. multiple linear regression)
- optimise (minimise) the loss function \rightarrow **optimiser**
- importance of the learning rate
- local minimum → momentum



Linear regression - recap







[minimise J(B) take derivatives and update parameters]

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Take away message



- linear regression from the machine learning perspective →a predictive machine
- to be able to make predictions, we first need to **estimate parameter coefficients**
- define a loss function and then use gradient descent to minimize it
- partial derivatives are used to **update** the values of the **parameters**
- **gradient descent** is a general method to minimise the loss (cost) function for a variety of machine learning models

Model evaluation



- we have our model
- we have estimated the parameters (coefficients) of the model
- we can now get predictions from our predictive machine

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Model evaluation



- we have our model
- we have estimated the parameters (coefficients) of the model
- we can now get predictions from our predictive machine

\rightarrow how good is our model?

(root) Mean squared error (MSE)



 $MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - f(x_i))^2$

average squared difference between predictions and observations

$RMSE = \sqrt{MSE}$

• on the same scale as the target variable

Mean absolute error (MAE)



$$MAE = rac{1}{n}\sum_{i=1}^n |y_i - f(x_i)|$$

less sensitive to outliers

and the normalized version:

$$NMAE = rac{MAE}{\overline{y}}$$

Correlations

- **Pearson's** linear correlation coefficient:
- **Spearman's** rank correlation coefficient:

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 $ho_{y,\hat{y}}$



Measuring performance



- Demonstration 1.2
- Exercise 1.2

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